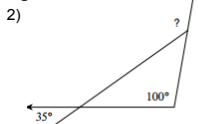
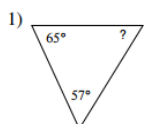
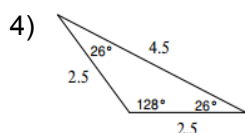
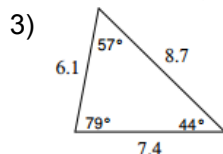


Find the missing angles.



Classify the triangles by sides and angles.  
acute, right, obtuse,  
scalene, isosceles, equilateral

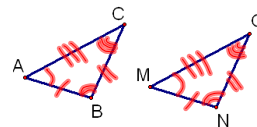


## 4.2 Apply Congruence and triangles

Congruent Triangles—same size and shape

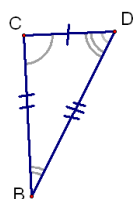
$$\triangle ABC \cong \triangle MNO$$

$$\begin{aligned} \angle A &\cong \angle M & \overline{AB} &\cong \overline{MN} \\ \angle B &\cong \angle N & \overline{BC} &\cong \overline{NO} \\ \angle C &\cong \angle O & \overline{AC} &\cong \overline{MO} \end{aligned}$$



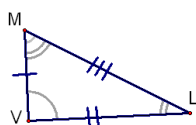
The corresponding parts of congruent triangles are congruent.

**CPCTC**



What triangles are congruent?

$$\triangle CBD \cong \triangle VLM$$



If  $\triangle THE \cong \triangle SAW$ , what parts are congruent?

$$\begin{aligned} \angle T &\cong \angle S \\ \angle H &\cong \angle A \\ \angle E &\cong \angle W \end{aligned}$$

$$\begin{aligned} \overline{TE} &\cong \overline{SW} \\ \overline{TH} &\cong \overline{SA} \\ \overline{HE} &\cong \overline{AW} \end{aligned}$$

Theorem 4.3—3<sup>rd</sup> Angle Theorem—If 2 angles of 1 triangle are  $\cong$  to 2 angles of another triangle, then the 3<sup>rd</sup> angles are  $\cong$ .

Theorem 4.4--Properties of Congruent Triangles

Reflexive  $\triangle ABC \cong \triangle ABC$

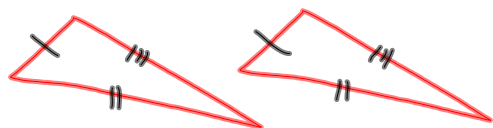
Symmetric If  $\triangle ABC \cong \triangle MNO$ , then  $\triangle MNO \cong \triangle ABC$

Transitive If  $\triangle ABC \cong \triangle MNO$  and  $\triangle MNO \cong \triangle XYZ$ , then

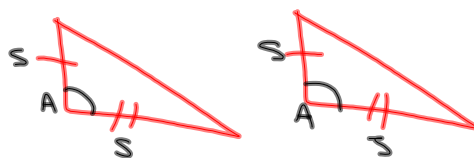
$$\triangle ABC \cong \triangle XYZ$$

4.3 Prove Triangles Congruent by SSS and SAS (section 4.4)

Postulate 19--Side-Side-Side(SSS)-If 3 sides of one  $\triangle$  are congruent to 3 sides of another  $\triangle$ , then the  $\triangle$ s are congruent.



Postulate 20--Side-Angle-Side(SAS)-If 2 sides and the included angle of one  $\triangle$  are congruent to 2 sides and the included angle of another  $\triangle$ , then the  $\triangle$ s are congruent.



Things to keep in mind for these proofs:

Reflexive

Vertical angles are congruent

Def. of midpoint

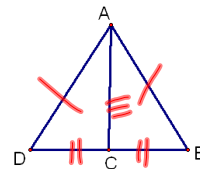
Def. of angle bisector and segment bisector

Parallel line facts

and anything else we have learned

Given:  $\overline{C}$  is the midpoint of  $\overline{DB}$   
 $\overline{AD} \cong \overline{AB}$

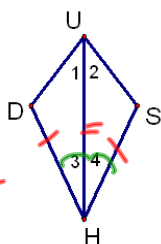
Prove:  $\triangle ADC \cong \triangle ABC$



S.	R.
① $C$ is midpoint $\overline{DB}$ $\overline{DC} \cong \overline{CB}$ ✓	① Given
② $\overline{DC} \cong \overline{CB}$ ✓	② def of midpoint
③ $\overline{AC} \cong \overline{AC}$ ✓	③ Reflexive
④	④ SSS

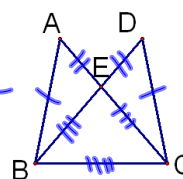
Given:  $\overline{HU}$  bisects  $\angle DHS$   
 $\overline{HD} \cong \overline{HS}$

Prove:  $\triangle UDH \cong \triangle USH$



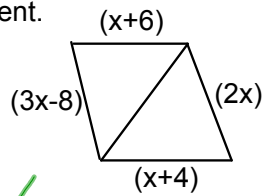
S.	R.
① $\overline{HU}$ bis. $\angle DHS$ $\overline{HD} \cong \overline{HS}$ ✓	① Given
② $\angle 3 \cong \angle 4$ ✓	② def of $\angle$ Bis
③ $\overline{UH} \cong \overline{UH}$	③ Reflexive
④ $\triangle UDH \cong \triangle USH$	④ SAS

Given:  $\overline{AB} \cong \overline{DC}$ ;  $\overline{AE} = \overline{DE}$ ;  $\overline{EB} = \overline{EC}$   
 Prove:  $\triangle ABC \cong \triangle DCB$



S.	R.
① $\overline{BC} \cong \overline{BC}$	① Given
② $\overline{BC} \cong \overline{BC}$	② Refl.
③ $\overline{DE} + \overline{EB} = \overline{DB}$ $\overline{AE} + \overline{EC} = \overline{AC}$	③ S.A.P.
④ $\overline{AE} + \overline{EC} = \overline{DE} + \overline{EB}$	④ Addition
⑤ $\overline{AC} = \overline{DB}$	⑤ Subst.
⑥ $\overline{AC} \cong \overline{DB}$	⑥ def of $\cong$
⑦ $\triangle ABC \cong \triangle DCB$	⑦ SSS

Find all values of  $x$  that make the triangles congruent.



$$\begin{array}{l}
 \cancel{x+6 = x+4} \\
 \quad 6 \neq 4 \\
 \cancel{3x-8 = 2x} \\
 \quad \text{not possible}
 \end{array}
 \quad
 \begin{array}{l}
 x+6 = 2x \\
 \quad 6 = x \\
 \quad x = 6
 \end{array}
 \quad
 \begin{array}{l}
 3x-8 = x+4 \\
 2x = 12 \\
 x = 6
 \end{array}$$

HW

p228-229

#s 3, 5-10, 16, 20

p236-238

#s 5-7, 21, 24, 26